## Math 11 Matrix Calculations

## Introduction

We are going to use Microsoft Excel to solve systems of equations.
We will use the following formulas:

- mdeterm - calculate matrix determinant
- minverse - calculate matrix inverse
- mmult - multiply matrices


## Part A

We will solve page 54 \#60 a):

$$
\begin{aligned}
& 5 x-8 y=-42 \\
& -3 x+5 y=26
\end{aligned}
$$

## Steps:

1. Open a new spreadsheet in Microsoft Excel.
2. Input the all the values from Picture \#1 into the appropriate cells. For example, in cell B3 insert 5, in cell C3 insert -8.

Picture \#1:

| B3 |  | $\square f \times \Sigma=5$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E | F | G |  |
| 1 |  |  |  |  |  |  |  |  |
| 2 |  | Coefficient Ma | trix |  | Solution Matrix |  |  |  |
| 3 |  | 5 | -8 |  | -42 |  |  |  |
| 4 |  | -3 | 5 |  | 26 |  |  |  |
| 5 |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |
| 7 |  | Determinant |  | Inverse |  |  | Solution |  |
| 8 |  |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |

3. In cell $\mathbf{C 8}$ enter the formula $=m \operatorname{determ}(B 3: C 4)$ and press the enter key.

Note: You can highlight the cells B3:C4 using the mouse instead of typing in B3:C4 and the program will automatically fill it in the formula for you.


In C8 you should now see the number 1. This is the determinant of the $2 x 2$ matrix.
4. With your mouse, highlight the cells D8,E8,D9,E9. Enter the following formula: =minverse (B3;C4). Press CTRL-SHIFT-ENTER. (Note ENTER will only populate one cell instead of 4.)

You should now see cells D8;E9 populated with the matrix inverse.

| D8:E9 |  | - $f_{\mathrm{x}} \Sigma^{\sim}=\{=\operatorname{MINVERSE}(\mathrm{B3}: \mathrm{C4})\}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E | F | G |
| 1 |  |  |  |  |  |  |  |
| 2 |  | Coefficient Mat |  |  | Solution Matrix |  |  |
| 3 |  | 5 | -8 |  | -42 |  |  |
| 4 |  | -3 | 5 |  | 26 |  |  |
| 5 |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |
| 7 |  | Determinant |  | Inverse |  |  | Solution |
| 8 |  | 1 |  | 5 | 8 |  |  |
| 9 |  |  |  | 3 | 5. |  |  |
| 10 |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |

5. With your mouse, highlight the cells G8 and G9. Enter the following formula $=m m u l t(D 8: E 9 ; E 3: E 4)$ and press CTRL-SHIFT-ENTER. Your field is now populated with the answer to your matrix equation. $(x=-2, y=4)$.

| G8:G9 |  | $\square f_{\mathbf{x}} \mathbb{E}=\left\{^{(=\mathrm{MMULT}}\right.$ (D8:E9;E3:E4) $\}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E | F | G |
| 1 |  |  |  |  |  |  |  |
| 2 |  | Coefficient Ma |  |  | Solution Matrix |  |  |
| 3 |  | 5 | -8 |  | -42 |  |  |
| 4 |  | -3 | 5 |  | 26 |  |  |
| 5 |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |
| 7 |  | Determinant |  | Inverse |  |  | Solution |
| 8 |  | 1 |  | 5 | 8 |  | -2 |
| 9 |  |  |  | 3 | 5 |  | 4 |
| 10 |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |

6. Try changing the values of the Coefficient Matrix and Solution Matrix for the numbers $60 \mathrm{~g}, \mathrm{~h}$, and i. Do they match your answers from your homework?

Answers: 60 g. (1,-2) h. (-40,-24) i. (6,-2)

## Part B

We solve $3 \times 3$ matrix equations the exact same way we solve $2 \times 2$ matrix equations, however the determinant and inverse of $3 \times 3$ matrices are usually too complicated to solve by hand.

Make a new excel file (or modify the one you have) to solve $3 \times 3$ equations. Use it to solve the following equations:
a. $x-3 y+5 z=-14$
$2 x+y-6 z=20$
b. $\begin{aligned}-2 x+4 y-z & =-7 \\ x+2 y+3 z & =-2 \\ 4 x-2 y+3 z & =14\end{aligned}$
c. $x+3 y-8 z=16$
$2 x+y-4 z=-6$
$3 x-2 y+z=0$
$-x+2 y+12 z=18$

Answers:
a) $(1,0,-3)$
b) $(6,1 / 2,-3)$ c) $(-7,7,-1 / 4)$

## Part C

Make a new excel file and perform a matrix multiplication on the following two charts below (Chart A $x$ Chart B).
a) Fill in Chart C below.
b) In your own words, what does your final answer represent?

## Chart A:

|  | Number of Cars Sold |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Salesperson Name |  | Civic Coupe | Civic Sedan | Civic Hybrid | Accord Coupe | Accord Sedan |
|  | Tom | 1 | 2 | 0 | 2 | 3 |
|  | Jerry | 2 | 4 | 1 | 0 | 0 |
|  | Beavis | 2 | 3 | 3 | 0 | 0 |

## Chart B:

|  | Car Price |
| :--- | :--- |
| Civic Coupe | $\$ 18240$ |
| Civic Sedan | $\$ 25990$ |
| Civic Hybrid | $\$ 24990$ |
| Accord Coupe | $\$ 26790$ |
| Accord Sedan | $\$ 24790$ |

## Chart C:



